# In celebration of the $60^{\text {th }}$ birthday of Dr. Andrew K. Galwey 

# THE TERNARY SYSTEM CsCl-NaCl-LaCl3 

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#### Abstract

The ternary system $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$ was investigated by means of differential thermal analysis and X-ray powder diffraction analysis. There exists one congruently melting compound, $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$, crystallizing with the cubic elpasolite structure. No quasi-binary section exists for the whole system, however three binaries range from the ternary compound $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ to NaCl , $\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ and $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ resp., dividing the system in three areas of composition: one triangle, $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$, containing additionally a compound $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$ below $510^{\circ} \mathrm{C}$, and the two areas $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ and $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{NaCl}_{2}-\mathrm{LaCl}_{3}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$, containing a mixed crystal range between $\mathrm{LaCl}_{3}$ and $\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$. These areas could be further divided in five triangles, so that the whole system contains six Alkemade triangles.


Keywords: DTA, ternary system $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$, XRD

## Introduction

Recently [1] we have reported on thermochemical investigations of chloro elpasolites of lanthanum. Four compounds $\mathrm{A}_{2} \mathrm{BLaCl}_{6}$ exist: $\mathrm{Cs}_{2} \mathrm{RbLaCl}_{6}$, $\mathrm{Cs}_{2} \mathrm{KLaCl}_{6}, \mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ and $\mathrm{Rb}_{2} \mathrm{KLaCl}_{6}$. Only the Cs -compounds are stable at ambient temperature. $\mathrm{Cs}_{3} \mathrm{RbLaCl}_{6}$ and $\mathrm{Cs}_{2} \mathrm{KLaCl}_{6}$ are polymorphous; $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ crystallizes from ambient temperature up to the (congruent) melting point at 930 K with the cubic aristotype structure in space group Fm3m [2].

In this paper we give the results of an investigation of the ternary system $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$, using differential thermal analysis (DTA) and X-ray diffraction measurements (XRD) on crystal powders. We have done this work as a basis for e.m.f.-measurements for determining the Gibbs-enthalpy, $\Delta G^{\circ}$, for the formation of $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ from either the compounds $\mathrm{CsCl}, \mathrm{NaCl}$ and $\mathrm{LaCl}_{3}$, or from NaCl and the binary compound, $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$. First we have ascertained the triangles of existence (compatibility triangles) at ambient temperature with Xray patterns of quenched and, if necessary, annealed samples of appropriate
composition. In a second step, suitable sections through the systems were measured with DTA. From the results of both methods the final diagram was constructed.

## Experimental

## Preparation of the compounds

For the preparation of anhydrous $\mathrm{LaCl}_{3}$, the hydrate $\mathrm{LaCl}_{3} \cdot 7 \mathrm{H}_{2} \mathrm{O}$, obtained from a solution of $\mathrm{La}_{2} \mathrm{O}_{3}$ (p.A., Fa. Merck) in hydrochloric acid, was treated in a vacuum oven at $60^{\circ} \mathrm{C}$ and then dehydrated by heating in a HCl -stream for one day, raising the temperature slowly from 100 to $700^{\circ} \mathrm{C}$. After subsequent cooling, all further manipulations were done in a glove-box. The alkaline metal chlorides (p.A., Fa. Merck) were dried in a HCl -stream at $500^{\circ} \mathrm{C}$.

The binary and ternary chloride compounds were obtained by melting adequate mixtures in vacuum-sealed ampoules using a gas flame. The melt was homogenized by shaking and solidified by rapid cooling.

## Differential thermal analysis

The home-built DTA device has already been described [3]. The samples $(1.5 \mathrm{~g})$ were prepared in the same way as described for the binary chlorides. The solids thus obtained were sufficiently homogeneous for the measurement of heating curves and for annealing experiments. Thermal effects could be detected down to 0.2 J for the generally used heating rate of $2 \mathrm{deg} \cdot \mathrm{min}^{-1}$.

All ternary samples on the investigated sections were mixed from the compounds at the corners and not from the compounds $\mathrm{CsCl}, \mathrm{NaCl}$ and $\mathrm{LaCl}_{3}$. Therefore we established the following expression for determining the molar composition, $\sigma$, of each sample:

$$
\sigma=\frac{t_{1}-X_{1} t}{X_{1}(s-t)+t_{1}-s_{1}}
$$

[^0]
Fig. 1 The binary systems $\mathrm{CsCl}-\mathrm{LaCl}_{3}$ and $\mathrm{NaCl}-\mathrm{LaCl}_{3}$


Fig. 2 The compatibility triangles
It must be pointed out that the temperatures in the binary systems $\mathrm{CsCl}-$ $\mathrm{LaCl}_{3}$ and $\mathrm{NaCl}-\mathrm{LaCl}_{3}$, previously measured [4], are 'onset-temperatures' from heating-curves and therefore 'kinetic-temperatures' which are in general too high, as we have discussed elsewhere [5]. For instance, for the phase-transition $\alpha-\beta-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ the temperature from heating-curves was found at $401^{\circ} \mathrm{C}$; in the ternary system $388^{\circ} \mathrm{C}$ was observed, probably under the catalytic effect of additional Na-containing compounds; recent e.m.f.-measurements gave a 'thermodynamic temperature' of $386^{\circ} \mathrm{C}$ [6]. Otherwise, the temperatures for the boundary curves are 'peak-temperatures' and, therefore, somewhat higher than the temperatures for the invariant points taken from onset-effects. This issue is known from binary systems too [5].

## $X$-ray diffraction

Powder patterns at ambient temperature were taken with a Philips PW 1050/25 goniometer equipped with a proportional counter and a vacuum attachment. During exposure ( $\mathrm{CuK}_{\alpha}$-radiation) the samples were under He atmosphere.


## Results

## The constituent binary systems

The system $\mathrm{CsCl}-\mathrm{NaCl}$ is purely eutectic [7]. The eutectic temperature is $486^{\circ} \mathrm{C}$ ( $65 \mathrm{~mol} \% \mathrm{CsCl}$ ). The phase diagrams of the (pseudo-) binary systems $\mathrm{CsCl}-\mathrm{LaCl}_{3}$ and $\mathrm{NaCl}-\mathrm{LaCl}_{3}$ were elucidated earlier by ourselves [4]. In the system $\mathrm{CsCl}-\mathrm{LaCl}_{3}$ (Fig. 1a) three compounds exist: $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ (congruently melting; solid state transition at $388^{\circ} \mathrm{C}$ ), $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$ (stable in the solid state up to $510^{\circ} \mathrm{C}$ ), $\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ (congruently melting at $706^{\circ} \mathrm{C}$ ). The system is shown in Fig. 1a in a revised form, taking into account the considerations given above. The system $\mathrm{NaCl}-\mathrm{LaCl}_{3}$ (Fig. 1b) is eutectic, containing a range of solid solutions from $\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$ to $\mathrm{LaCl}_{3}$, up to $\sim 710^{\circ} \mathrm{C}$.


Fig. 4 Composition of samples for DTA measurements with their related sections
The compatibility triangles (Fig. 2)
The system $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$ with four binary compounds and the ternary elpasolite (abbr. Q) can be subdivided in seven triangles, which describe (at ambient temperature) equilibrium areas of in each case three compounds, the sides
are the two-phase-lines of the compounds at the corners they connect. Eleven possibilities for such a triangulation exist. For instance, in the area $\mathrm{CsCl}-\mathrm{NaCl}-$ $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ two diagonal equilibrium lines are possible: the line $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{NaCl}$ or $\mathrm{CsCl}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$. Which is real can be decided by an X-ray pattern of a sample with the composition of the intersection of the two lines (point III in Fig. 2): in the first case it must consist of $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ and NaCl , in the second case of CsCl and $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$. To ensure equilibrium composition, the sample was quenched from the melt and then annealed at $\sim 380^{\circ} \mathrm{C}$.

Six X-ray measurements (Fig. 3) were necessary, but also sufficient. Only point I Fig. 2 was not an intersection of possible triangle sides. The line $\mathrm{Cs}_{3} \mathrm{LaCl}_{5}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ is drawn interrupted, because the compound $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$ has a solid state decomposition at $510^{\circ} \mathrm{C}$. Therefore no primary solidification area exists for this compound.

## DTA investigations

All DTA measurements and the related sections are collected in Fig. 4. With two exceptions, all sections extend between two compounds. The remaining two sections were selected in order to cover the system evenly with sections and to enable the determination of all ternary eutectic points. DTA investigations revealed that three of the seven equilibrium lines, all starting from the quaternary compound $Q$, are quasi-binary sections. The three phase diagrams for them $\left(Q-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}, Q-\mathrm{NaCl}\right.$ and $\left.Q-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}\right)$ are shown in Fig. 5. Thus we have to deal with three areas which are independent, since they do not contain any compound from outside. These are: a) the triangle $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-Q-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$, b) the quadrangle $\mathrm{CsCl}-\mathrm{NaCl}-Q-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ and c) the quadrangle $Q-\mathrm{NaCl}-$ $\mathrm{LaCl}_{3}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$.

## The area $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$

In addition to the phase diagrams $\mathrm{CsCl}-\mathrm{LaCl}_{3}$ (Fig. 1a), $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-Q$ and $Q_{-}$ $\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ (Fig. 5), we have used the diagram, given in Fig. 6a, to construct the liquid-solid diagram for the triangle. The result is depicted in Fig. 7: Starting from the binary eutectic $e_{3}$ and the saddle-points of Fig. 5a and 5c, the three boundary curves converge in the invariant point $E_{3}$, a ternary eutectic. It must be pointed out that below $510^{\circ} \mathrm{C}$ a further compound, $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$, is formed, stable only in the solid state.

Fig. 5 Phase diagrams for the quasi-binary secting from $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}(\mathrm{Q})$ : a) $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$, b) $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{NaCl}$,
c) $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$

Fig. 6 Phase diagrams: a) $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6} / \mathrm{Cs}_{3} \mathrm{LaCl}_{6}(52: 48)-\mathrm{CsLaCl}_{7}$, b) $\mathrm{CsLa}_{2} \mathrm{Cl}_{7}-\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$

## The area $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$

In addition to the edge diagrams $\mathrm{CsCl}-\mathrm{NaCl}, \mathrm{CsCl}-\mathrm{LaCl}_{3}$ (Fig. 1a), $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-$ $Q$ (Fig. 5a) and $Q-\mathrm{NaCl}$ (Fig. 5b), two further diagrams were used: $\mathrm{CsCl}-Q$ and $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{NaCl}$ (Fig. 8). Two valleys (boundary curves), starting from the saddlepoints of Fig. 5 a and 5 b , converge in the ascending fork-point (semi-eutectic point) $\mathrm{U}_{1}$. From there and from the eutectic $\mathrm{e}_{1}$ and $\mathrm{e}_{4}$ three boundary curves run together in the ternary eutectic $E_{1}$.

## The area $\mathrm{Cs}_{3} \mathrm{LaCl}_{5}-\mathrm{NaCl}-\mathrm{LaCl}_{3}-{\mathrm{Cs} \mathrm{Ca}_{2} \mathrm{Cl}_{7}}$

In this area, a complication exists in the solid state, concerning the mixed crystal range between $\mathrm{LaCl}_{3}$ and $\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$. We have neglected this and have treated the system $\mathrm{NaCl}-\mathrm{LaCl}_{3}$ (Fig. 1b) as if only the peritectic would exist at $-710^{\circ} \mathrm{C}$. The DTA measurements used for the construction of the liquid-solid surface can be taken from Fig. 4. The phase diagrams of the sections, not yet described, are given in Figs 6 b and 9. An ascending fork-point $\mathrm{U}_{3}$ is formed by two valleys, coming down from the binary peritectic $u 1$ and $u_{2}$. From there and from the saddle-point of the section $Q-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ (Fig. 5c) a further ascending fork-point, $\mathrm{U}_{2}$, is reached. The lowest invariant point of the whole quadrangle, the ternary eutectic $\mathrm{E}_{2}$, is the meeting point of valleys from $\mathrm{U}_{2}$, the saddle-point of the section $Q-\mathrm{NaCl}$ and the eutectic $\mathrm{e}_{2}$ from the edge system $\mathrm{NaCl}-\mathrm{LaCl}_{3}$.


Fig. 7 Boundary curves in the ternary system $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$

Fig. 8 Phase diagrams: a) $\mathrm{CsCl}^{2}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$, b) $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{NaCl}$

Fig. 9 Phase diagrams of sections from $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ to a) $\mathrm{LaCl}_{3}$, b), $\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$


Fig. 9 Phase diagrams of sections from $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ to c) $\mathrm{NaCl} / \mathrm{LaCl}_{3}$ (70:30) and d) $\mathrm{CsLa}_{2} \mathrm{Cl}_{7}-\mathrm{NaCl}$

## Conclusion

The ternary phase diagram $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$ with some main isotherms shown in Fig. 10. In Table 1 the compositions and the temperatures of the invariant points are complied.


Fig. 10 The system $\mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$
Table 1 Compositions and temperatures of the ternary invariant points (For the binary systems see Fig. 1)

|  | $\mathrm{mol} \%$ |  |  |  |
| :--- | :---: | :---: | :---: | :--- |
|  | $\mathrm{LaCl}_{3}$ | NaCl | $t{ }^{\circ} \mathrm{C}$ | Reaction |
| $\mathrm{U}_{1}$ | 8 | 37 | 545 | $\mathrm{~L}+\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6} \rightarrow \mathrm{Cs}_{3} \mathrm{LaCl}_{6}+\mathrm{NaCl}$ |
| $\mathrm{U}_{2}$ | 41 | 45 | 499 | $\mathrm{~L}+\mathrm{CsLa}_{2} \mathrm{Cl}_{7} \rightarrow \mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}+\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$ |
| $\mathrm{U}_{3}$ | 57 | 22 | 615 | $\mathrm{~L}+\mathrm{LaCl}_{3} \rightarrow \mathrm{CsLa}_{2} \mathrm{Cl}_{7}+\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$ |
| $\mathrm{E}_{1}$ | 5 | 29 | 475 | $\mathrm{~L} \rightarrow \mathrm{CsCl}+\mathrm{NaCl}+\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ |
| $\mathrm{E}_{2}$ | 36 | 48 | 492 | $\mathrm{~L} \rightarrow \mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}+\mathrm{NaCl}^{2}+\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$ |
| $\mathrm{E}_{3}$ | 45 | 10 | 532 | $\mathrm{~L} \rightarrow \mathrm{Cs}_{3} \mathrm{LaCl}_{6}+\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}+\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ |

Concerning the liquid-solid surfaces, there are three binaries: $\mathrm{NaCl}-$ $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}, \mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ and $\mathrm{CsLa}_{2} \mathrm{Cl}_{7}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$. The other composition joints are ternary sections in the system. However, below $510^{\circ} \mathrm{C}$, the temperature for the formation of $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$, the section $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}-\mathrm{NaCl}$ is built up of two solid phase regions: $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ and $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-$ NaCl . Thus, it must be possible to construct a galvanic cell for solids in which the reaction $\mathrm{NaCl}+\mathrm{Cs}_{2} \mathrm{LaCl}_{5}=\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$ is performed. However, it is absolutely necessary to use a compound $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$ with exact stoichiometric composition; otherwise one would come into three-phase regions with an additional compound of the binary system $\mathrm{CsCl}-\mathrm{LaCl}_{3}$.

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Zusammenfassung - Das ternäre $\operatorname{System~} \mathrm{CsCl}-\mathrm{NaCl}-\mathrm{LaCl}_{3}$ wurde mittels Differenzthermoanalyse und Röntgenbeugungsmessungen an Kristallpulvern untersucht. Es existiert eine kongruent schmelzende Verbindung $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}$, die im kubischen Elpasolith-Typ kristallisiert. Es liegt kein quasibinärer Schnitt für das gesamte System vor, jedoch drei solcher Teilschnitte, die von der ternären Verbindung $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6} \mathrm{zu} \mathrm{NaCl}, \mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ bzw. $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ verlaufen. Sie unterteilen das System in ein Dreieck $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$, das zusätzlich eine nur unterhalb von $510^{\circ} \mathrm{C}$ stabile Verbindung $\mathrm{Cs}_{2} \mathrm{LaCl}_{5}$ enthält, sowie die zwei Gebiete $\mathrm{CsCl}-\mathrm{NaCl}-$ $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$ und $\mathrm{Cs}_{2} \mathrm{NaLaCl}_{6}-\mathrm{NaCl}-\mathrm{LaCl}_{3}-\mathrm{CsLa}_{2} \mathrm{Cl}_{7}$ mit einem Mischkristallgebiet zwischen $\mathrm{LaCl}_{3}$ und $\mathrm{Na}_{3} \mathrm{La}_{5} \mathrm{Cl}_{18}$. Die beiden genannten Gebiete lassen sich in fünf Dreiecke zerlegen, so dass das ternäre System insgesamt sechs Kompatibilitätsdreiecke enthält.


[^0]:    E.g., a sample on the section $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}-\mathrm{NaCl}$ which contains $60 \mathrm{~mol} \% \mathrm{CsCl}$.

    Left corner $\left(\mathrm{Cs}_{3} \mathrm{LaCl}_{6}\right): s_{1}=3, s_{2}=0, s_{3}=1$ and $s=s_{1}+s_{2}+s_{3}=4$
    right corner ( NaCl ): $t_{1}=0, t_{2}=1, t_{3}=0$ and $t=t_{1}+t_{2}+t_{3}=1$,
    desired concentration of $\mathrm{CsCl}: X_{1}=0.6$;
    this leads to $\sigma=0.5$, which means that the sample contains $50 \mathrm{~mol} \%$ $\mathrm{Cs}_{3} \mathrm{LaCl}_{6}$

